

ECE 6095

Problem Set # 2

(Due September 18, 2012)

(Homework can be done in teams of two students. Use MATLAB when necessary)

- In this problem, we go through a step-by-step process for computing the torque and efficiency of an induction motor. Consider the equivalent circuit of a 460-V, 25-hp¹, 60 Hz, four-pole, Y-connected induction motor shown in Figure 1 with the impedances parameters in ohms per phase referred to the stator circuit as follows:

$$R_1 = 0.641\Omega, \quad R_2 = 0.332\Omega$$

$$X_1 = 1.106 \Omega, \quad X_2 = 0.464 \Omega, \quad X_M = 26.3 \Omega$$

The total frictional and rotational losses, P_{FR} , are 1100 W and are assumed to be constant. The core loss is lumped in with the rotational losses.

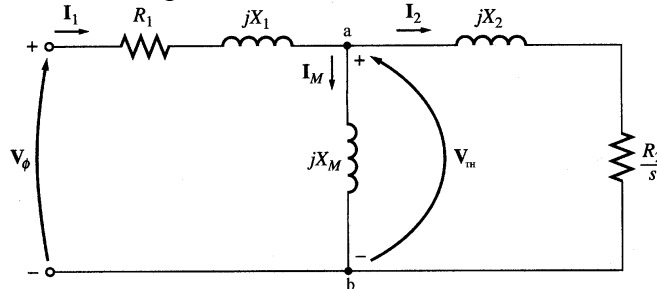


Figure 1: Equivalent Circuit of an Induction Motor

Find the synchronous speed in rpm, n_s and radian frequency, ω_s . For a rotor slip of 2.2 percent at the rated voltage and rated frequency, find the motor's (a) Speed in rpm, n_m and radian frequency, ω_m ; (b) Stator current, I_1 (c) Power factor (cosine of the angle, θ of stator current, I_1), (d) Input power, $P_{in} = \sqrt{3}V_\phi I_1 \cos \theta$, (e) stator core losses, $P_{SCL} = 3I_1^2 R_1$, (f) air gap power, $P_{AG} = P_{in} - P_{SCL}$, (g) Converted power, $P_{conv} = (1-s) P_{AG}$, where s is the slip, (h) output power, $P_{out} = P_{conv} - P_{FR}$, (i) efficiency, $\eta = P_{out} / P_{in}$ and (j) output torque, $T_{out} = \frac{P_{out}}{\omega_m}$.

- (Background) Show that for a continuous state variable feedback system

$$\dot{\underline{x}}(t) = \underline{A}\underline{x}(t) + \underline{B}\underline{u}(t), \quad \underline{u}(t) = \underline{K}_r r(t) - \underline{K}_c \underline{x}(t)$$

the loop gain is given by $LG(s) = \underline{K}_c (sI - \underline{A})^{-1} \underline{B}$. For the single input system, if

$$\underline{A} = \begin{bmatrix} 1 & 1 \\ -3 & 0 \end{bmatrix} \quad \underline{B} = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \quad \underline{K}_c = [\alpha \quad 3]$$

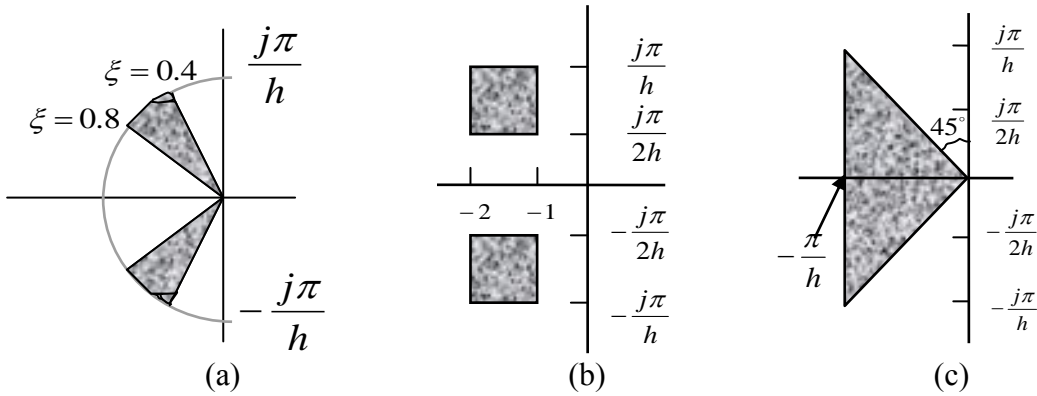
¹ 1hp = 746 watts

for what range of α is the closed-loop system stable? For $\alpha = 2$ what is the crossover frequency ω_c and the phase margin ϕ_m of the closed-loop system?

3. What are the points in the z -plane that correspond to the following points in the s -plane when $h = 0.628$?

- (a) $s = -2$ (b) $s = -8$ (c) $s = 1$
 (d) $s = -2 + j2$ (e) $s = -2 + j7$ (f) $s = -j5$
 (g) What point(s) in the s -plane correspond to $z = -0.5$?

4. What region in the z -plane corresponds to the following regions in the s -plane $z = e^{sh}$ when $h = 0.25$ sec



5. Consider the all pass filter $H_{ap}(z) = \frac{1-az}{z-a}$; $|a| < 1$ (poles and zeros are mirror images around unit circle). These will be useful in loop shaping. By evaluating $H(e^{j\omega})H(e^{-j\omega})$ or $H(z)H(z^{-1})$, show that the magnitude is one. Determine an expression for the phase angle of $H_{ap}(z)$.